

- 1) Use substitution to calculate  $I = \iint_R \frac{(x-y)^2}{\sqrt{x+y}} dx dy$  if  $R$  is the region in the  $xy$ -plane bounded by  $x+y=1$ ,  $x+y=2$ ,  $x-y=1$ , and  $x-y=-1$ . (7 points)

- 2) Find the mass of the surface  $S$  parameterized by  $\vec{\alpha}(u, p) = \langle \cos u, \sin u, \sin p \rangle$  for  $0 \leq u \leq \frac{\pi}{2}$ , and  $0 \leq p \leq \frac{\pi}{2}$  if the density is  $\delta(x, y, z) = x^2 + y^2 + z^2$  grams per square meter. (6 points)

3) Find the flux of  $\vec{F}(x, y, z) = \langle 2x + y, x - 2y, 2 \rangle$  through the graph of  $f(x, y) = 2x^2 - 2xy - 2y^2$ , oriented up, if  $1 \leq x^2 + y^2 \leq 4$ . (6 points)

4) Find the flux of  $\vec{F}(x, y, z) = \langle x, z, y \rangle$  through the piece of the cylinder  $x^2 + y^2 = 4$  that lies in the first octant below  $z = 5$ . This surface is oriented away from the  $z$ -axis. (6 points)